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Grade/Class : 12/..... Mathematics Teacher :

150

ANSWER BOOKLET

Paper 2

12 June 2017

QUESTION 1

1	2	3	4	5	6	7	8	9	10	11	12	13
17	20	21	25	29	30	35	41	56	60	70	85	88

M

1.1.	1.1. $\bar{x} = 44,38$ ✓	1
1.1.	1.2. $M = T_{\frac{1}{2}}(1+13)$	
	$= T_7$	
	$= 35$ ✓	1
1.1.	2. $\bar{x} - M = 44,38 - 35$ ✓	
	$= 9,38$	
	> 0	
	\therefore data is <u>positively skewed</u> (skewed to the right)	2

1,2.	1. $\sigma = 23,85$ ✓ →	1
2.	$\bar{x} - \sigma$ $\bar{x} + \sigma$	
	$= 44,38 - 23,85$ $= 44,38 + 23,85$	
	$= 20,53$ $\checkmark^{607 \text{ bis}}$ $= 68,23$	
	$\therefore \frac{\textcircled{8}}{13} \times 100$ ✓	
	$= 61,54\%$ ✓ →	3

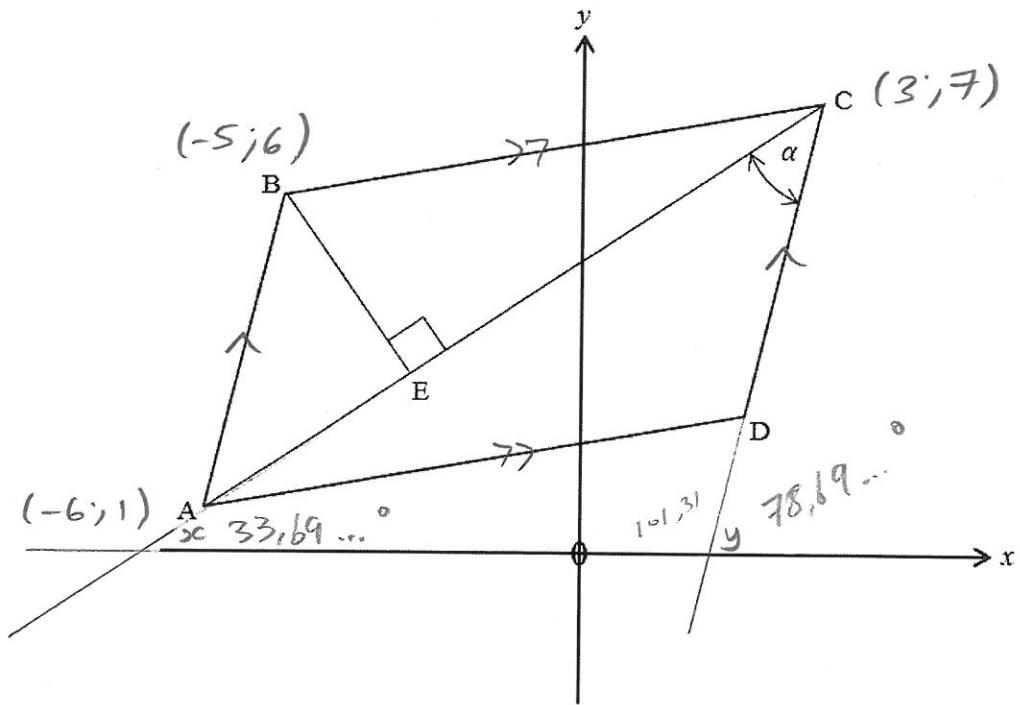
QUESTION 2

2.1.	$63 \checkmark$ learners →	1
2.2.	$a = 10 - 0 = 10 \checkmark$ $b = 57 - 42 = \frac{15}{\longrightarrow} \checkmark$	2
2.3.	$40 < x \leq 50 \checkmark$ →	1
2.4.	$\leq 53 = 47 \checkmark$ $\therefore > 53 = 63 - 47$ $= \underline{16} \checkmark \pm 1$	2

QUESTION 3

3.1.	$a = 0,90 \checkmark$	
	$b = 0,85 \checkmark$	
	$\therefore y = 0,90 + 0,85x \checkmark$ →	2
3.2.	<u>Yes</u> , $r = 0,87 \checkmark$ reflecting a strong correlation.	2
3.3.	$30 = 0,90 + 0,85x$ $x = 34,23 \dots$ $\approx \underline{34} \checkmark$	1

QUESTION 4



4.1.	1. $m_{AC} = \frac{7 - 1}{3 - (-6)} = \frac{2}{3}$	$A(-6; 1) \quad C(3; 7)$
	$y = \frac{2}{3}x + c$	
	sub $A(-6; 1)$	
	$1 = \frac{2}{3}(-6) + c \quad \checkmark$	
	$5 = c$	
	$\therefore y = \frac{2}{3}x + 5 \quad \checkmark$	3
4.1.	2. $m_{BE} = -\frac{3}{2} \quad \checkmark$	$B(-5; 6) \quad E$
	$y = -\frac{3}{2}x + c$	
	sub $B(-5; 6)$	

	$6 = -\frac{3}{2}(-5) + c \quad \checkmark$	
	$-\frac{3}{2} = c$	
	$\therefore y = -\frac{3}{2}x - \frac{3}{2} \quad \checkmark$	3
4.2.	$y = \frac{2}{3}x + 5$	$y = -\frac{3}{2}x - \frac{3}{2}$
	Solving Simult.	
	$\frac{2}{3}x + 5 = -\frac{3}{2}x - \frac{13}{2} \quad \checkmark$	
	$\frac{13}{6}x = -\frac{13}{2} \quad \checkmark$	
	$x = -\frac{13}{2} \div \frac{13}{6}$	
	$= -3$	
	$\therefore y = \frac{2}{3}(-3) + 5 \quad \checkmark$	
	$= 3$	
	$\therefore E(-3; 3)$	3
4.3.	1. AC	$A(-6; 1) C(3; 7)$
	$= \sqrt{(7-1)^2 + (3-(-6))^2} \quad \checkmark$	
	$= \sqrt{117} \quad \checkmark$	2
4.3.	2. BE	$B(-5; 6) E(-3; 3)$
	$= \sqrt{(3-6)^2 + (-3-(-5))^2} \quad \checkmark$	
	$= \sqrt{13} \quad \checkmark$	1
4.4	Area $\Delta ABC = \frac{1}{2} \sqrt{117} \sqrt{13}$	
	$= \frac{39}{2} \quad \checkmark$	

but $\Delta ABC \cong \Delta DCA$ SSS

\therefore area $\text{l}gm ABCD$

$$= 2 \times \frac{39}{2}$$

$$= 39 \text{ units}^2$$

3

4.5. $\tan x = \frac{2}{3}$ ✓

$$x = 33,69\dots^\circ$$

$$m_{AB} = \frac{6-1}{-5-(-6)}$$

A(-6; 1) B(-5; 6)

$$= 5$$

$$= m_{CD}$$

opp sides \parallel gm \parallel

$$\tan y = 5$$

$$y = 78,69\dots^\circ$$

$$x + 33,69\dots^\circ = 78,69\dots^\circ \text{ ext } ^\wedge \Delta$$

$$\therefore x = 45^\circ$$

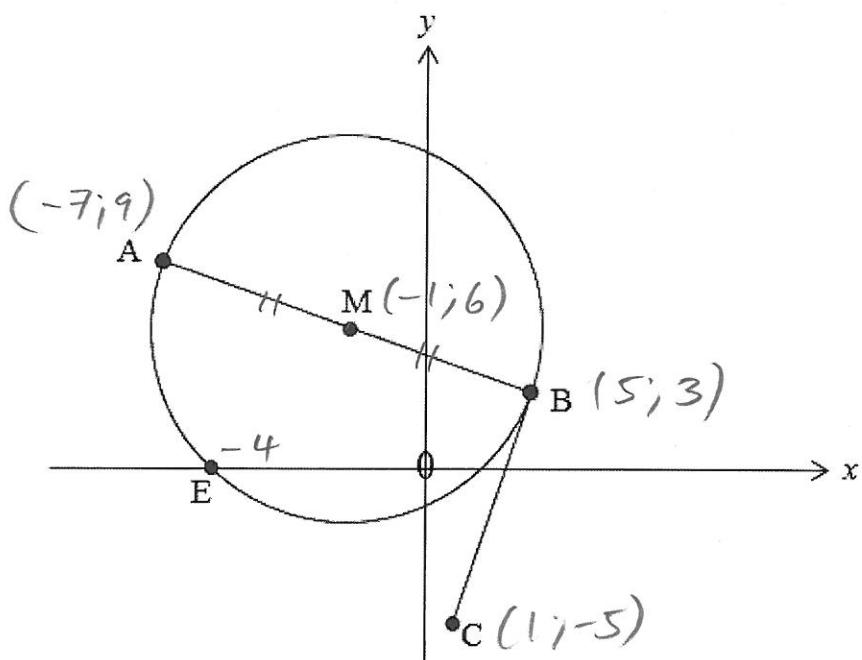
5

4.6. $B(-5; 6) \xrightarrow[\substack{1 \\ \uparrow}]{8 \rightarrow} C(3; 7)$

$$A(-6; 1) \xrightarrow[\substack{1 \\ \uparrow}]{8 \rightarrow} D(2; 2)$$

2

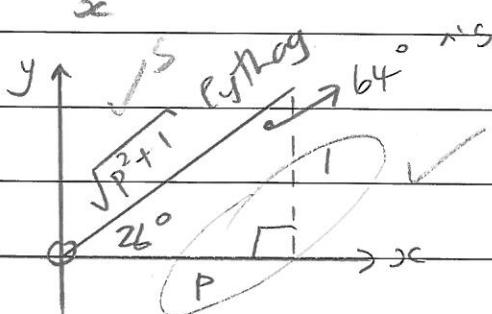
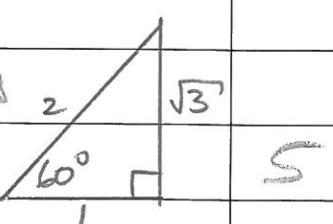
QUESTION 5



S.I.	1. $M(-1; 6)$ ✓	1
S.I.	2. $\frac{x_A + 5}{2} = -1 \quad \frac{y_A + 3}{2} = 6$	
	$x_A = \checkmark \quad y_A = \checkmark$	
	$\therefore A(-7; 9)$ ✓	2
S.I.	3. $x_{\text{int}}: (x+1)^2 + (0-6)^2 = 45$	
	$(x+1)^2 = 9 \checkmark$	
	$x+1 = \pm 3$	
	$\therefore x+1 = -3 \checkmark$	
	$x = -4$	
	$\therefore E(-4; 0) \checkmark$	3

5.2.	$m_{BC} = \frac{-5 - 3}{1 - 5}$ = 2 ✓	$B(5; 3) C(1; -5)$
	$m_{MB} = \frac{6 - 3}{-1 - 5}$ = $-\frac{1}{2}$ ✓	$B(5; 3) M(-1; 6)$
	$m_{BC} \times m_{MB} = 2 \times -\frac{1}{2}$ = -1 ✓	
	$\therefore BC \perp MB$	
	$\therefore BC$ is a $\sqrt{5}$ ^{SR} conv tangent \perp rad	5
5.3.	$m_{BC} = 2$	$D(d; -7\frac{5}{6}) B(5; 3)$
	$m_{BC} = m_{DB}$ $2 = \frac{3 - (-7\frac{5}{6})}{5 - d} \sqrt{m_{DB}}$ $2(5 - d) = \frac{65}{6}$ $d = -\frac{5}{12}$ ✓	3
5.4.	$(-1; 6) \xrightarrow{2\uparrow} (-1; 8)$	
	$r = \sqrt{45} \xrightarrow{x^2} r = 2\sqrt{45}$	
	$(x+1)^2 + (y-8)^2 = (2\sqrt{45})^2$	
	$(x+1)^2 + (y-8)^2 = 180$	2

QUESTION 6

6.1.	$\sin(A-B)$ $= \cos(90^\circ - (A-B)) \quad \checkmark$ $= \cos(90^\circ - A + B)$ $= \cos((90^\circ - A) - (-B)) \quad \begin{array}{l} \text{set up} \\ \text{and} \end{array} \checkmark$ $= \cos(90^\circ - A)\cos(-B) + \sin(90^\circ - A)\sin(-B) \quad \begin{array}{l} \text{expand} \\ \text{all reductions} \end{array}$ $= (\sin A)(+\cos B) + (\cos A)(-\sin B) \quad \begin{array}{l} \text{shown} \\ \text{shown} \end{array}$ $= \sin A \cos B - \cos A \sin B \quad \rightarrow \quad 3$
6.2.	$p \tan 26^\circ - 1 = 0$ $\tan 26^\circ = \frac{1}{p} \quad \frac{y}{x}$  $\sin 86^\circ = \sin(60^\circ + 26^\circ)$ $= \sin 60^\circ \cos 26^\circ + \cos 60^\circ \sin 26^\circ$ $= \left(\frac{\sqrt{3}}{2}\right)\left(\frac{1}{\sqrt{p^2+1}}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{\sqrt{p^2+1}}\right)$ <p>26° ratios ✓ 60° ratios ✓ lose it no →</p> 

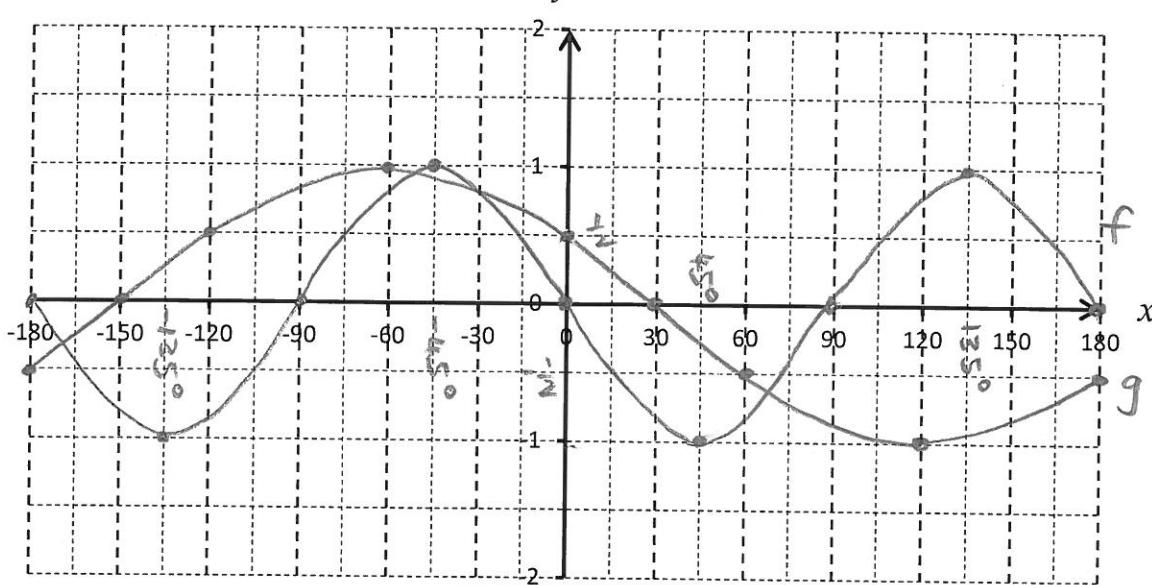
	$6.2. \quad 2. \quad \cos 2x = 1 - 2 \sin^2 x$ $\cos 26^\circ = 1 - 2 \sin^2 13^\circ \checkmark$ $\sqrt{\frac{P}{P^2+1}} = 1 - 2 \sin^2 13^\circ \checkmark$ $\sin 13^\circ = \sqrt{\frac{\frac{P}{\sqrt{P^2+1}} - 1}{-2}} \checkmark \quad 3$	
6.2.	$3. \quad \tan 296^\circ$ $= \tan 296^\circ \checkmark$ $= \tan (360^\circ - 64^\circ)$ $= -\tan 64^\circ \checkmark$ $= -\frac{P}{1} \quad \frac{0}{a}$ $= -P \quad \checkmark \quad 3$	
6.3.	$\cos(-x) = \cos x \quad \checkmark$ $\cos 2x = 2\cos^2 x - 1$ $\frac{3}{5} = 2\cos^2(-x) - 1 \quad \checkmark$ $\cos^2(-x) = \frac{4}{5}$ $\cos(-x) = \pm \sqrt{\frac{4}{5}} \quad \checkmark \quad 3$	
	$(\sqrt{\frac{4}{5}} = \frac{\sqrt{4}}{\sqrt{5}} = \frac{2}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{2\sqrt{5}}{5})$	

QUESTION 7

turning points
intercepts with
axrs

MUST BE
CLEARLY
LABELLED

7.1.



$$f: y = -\sin 2x$$

$$g: y = \cos(x+60^\circ)$$

✓ yint ✓ penalise if \pm not labelled

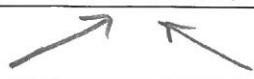
✓ xint ✓

penalise if
 $x = \pm 45^\circ$ and $\pm 135^\circ$ ✓ tp ✓
not labelled

6

7.2.	1. $P_f : y \in [-1; 1] \rightarrow$	1
7.2.	2. $\text{Period}_f = \frac{360^\circ}{2} = 180^\circ \rightarrow$	1
7.3.	1. $f(x) = g(x)$ $-\sin 2x = \cos(x+60^\circ)$ $A = 2x \quad B = 60^\circ$	

$$-\sin A = \cos B$$



$$\cos(90^\circ + A) \quad \cos(270^\circ - A) \quad (k \in \mathbb{Z})$$

II

III

$$\cos(90^\circ + A) = \cos B \quad \text{or} \quad \cos(270^\circ - A) = \cos B$$

$$90^\circ + A = B + k \cdot 360^\circ$$

$$90^\circ + 2x = x + 60^\circ + k \cdot 360^\circ$$

$$x = \checkmark -30^\circ + k \cdot 360^\circ$$

$$270^\circ - A = B + k \cdot 360^\circ$$

$$270^\circ - 2x = \checkmark x + 60^\circ + k \cdot 360^\circ$$

$$-3x = -210^\circ + k \cdot 360^\circ$$

$$x = \checkmark 70^\circ + k \cdot 120^\circ \quad 5$$

$$7.3. 2. \quad x \in [-180^\circ; 180^\circ] :$$

$$x ; -30^\circ ; x$$

$$x ; -170^\circ ; -50^\circ ; 70^\circ ; x$$

$$f(x) > g(x)$$

$$y_f > y_g$$

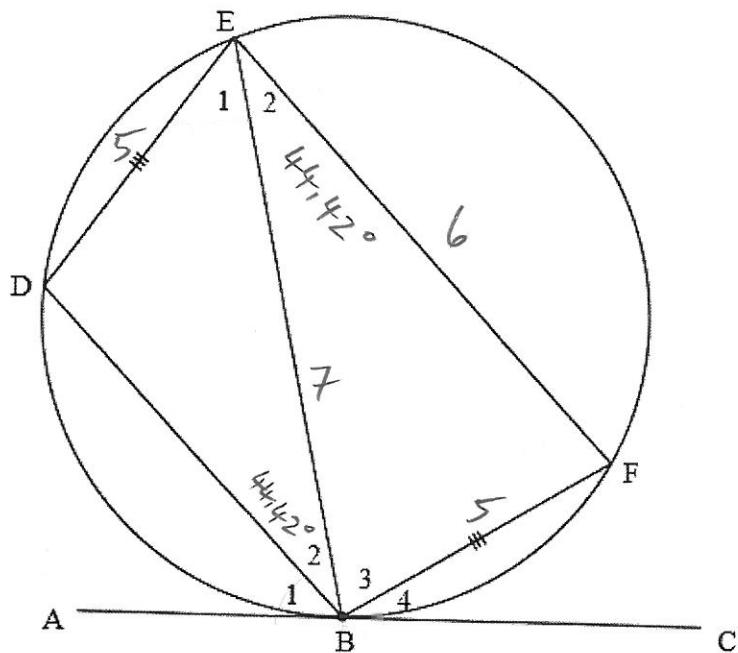
$$x \in [-180^\circ; -170^\circ) \text{ or } (-50^\circ; -30^\circ) \text{ or } (70^\circ; 180^\circ] \quad 3$$

$\checkmark A$

$\checkmark A$

$\checkmark A$

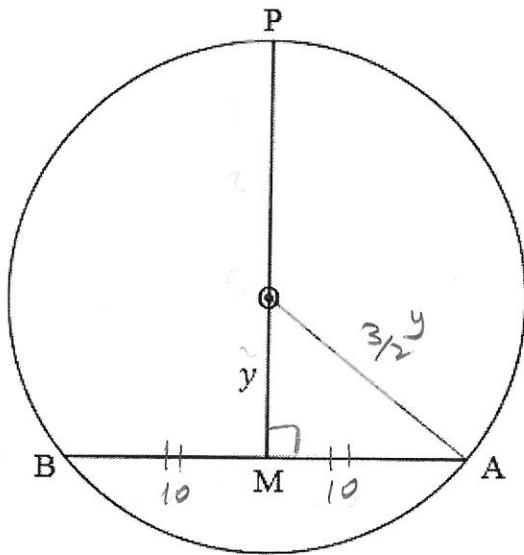
QUESTION 8



8.1.	$s^2 = 6^2 + 7^2 - 2 \cdot 6 \cdot 7 \cdot \cos \hat{E}_2 \quad \checkmark$ $84 \cdot \cos \hat{E}_2 = 60$ $\cos \hat{E}_2 = \frac{5}{7} \quad \checkmark$ $\hat{E}_2 = 44,42^\circ \quad \checkmark$	3
8.2.	$\hat{B}_2 = 44,42^\circ \quad \checkmark$ $\frac{\sin \hat{D}}{7} = \frac{\sin 44,42^\circ}{5} \quad \checkmark$ $\sin \hat{D} = 0,97 \dots \quad \checkmark$ $\text{ref } \hat{D} = 78,48\dots^\circ$ $\sin + \text{ in}$	
	I: x	
	II: $\hat{D} = 101,51\dots^\circ \quad \hat{D} > 90^\circ$	

	$\therefore \hat{E}_1 = 34,06\dots^\circ$ ✓ ^s ^f ^{is} $\Delta = 180^\circ$	
	$\therefore \hat{B}_1 = 34,07^\circ$ ✓ ^s ^f ^{is} $\tan \text{ chord}$	8

QUESTION 9



9.1.	$MA = 10 \sqrt{5}$ given	1
9.2.	line from centre O to midpt chord \sqrt{R}	1
9.3.	$\frac{PM}{OM} = \frac{5}{2}$ $PM = \frac{5}{2} OM$ $= \frac{5}{2} y \checkmark$	
	$OP = PM - OM$	
	$= \frac{5}{2} y - y$	
	$= \frac{3}{2} y \checkmark$	
	$= OA$ radius	

	$y^2 + 10^2 = \left(\frac{3}{2}y\right)^2$ ✓ $y^2 + 100 = \frac{9}{4}y^2$ $100 = \frac{5}{4}y^2$ $80 = y^2$ $y = \pm \sqrt{80}$ $= \sqrt{80}$ reject - $\underline{= 8,94} \quad \checkmark$	
--	--	--

Q 9.3.

alternative

$$9.3. \quad \frac{PM}{OM} = \frac{5}{2}$$

let $PM = 5x$ and $OM = 2x$

\equiv NOT $5y$ and $2y$
as y is
given in
diagram!

$$\therefore y = 2x \quad OM$$

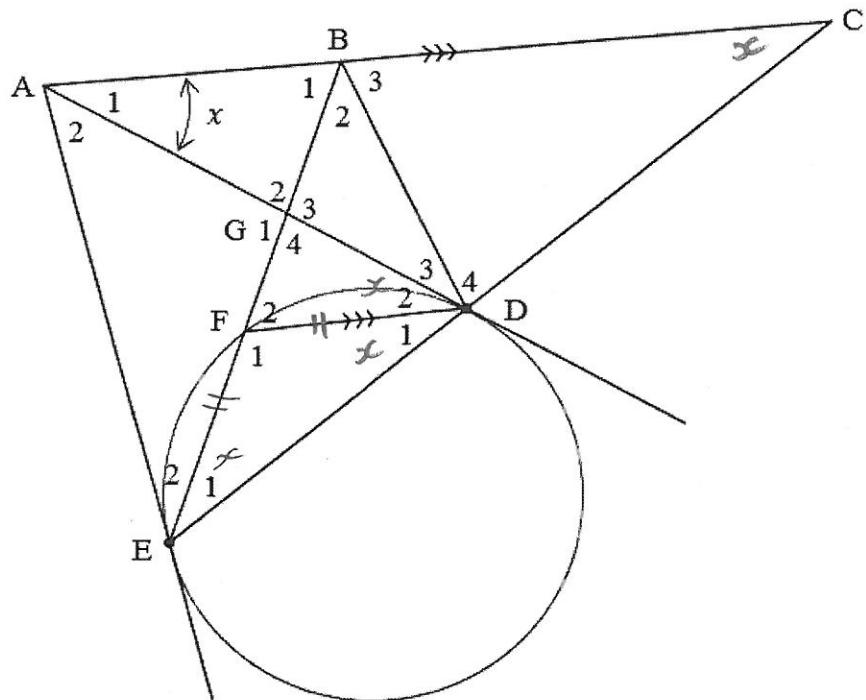
$$\begin{aligned} \therefore OP &= 5x - 2x \\ &= 3x \\ &= OA \quad \text{radius} \end{aligned}$$

$$\begin{aligned} OA^2 &= OM^2 + MA^2 \quad \text{pythag} \\ (3x)^2 &= (2x)^2 + (10)^2 \\ 9x^2 &= 4x^2 + 100 \\ 5x^2 &= 100 \\ x^2 &= 20 \\ x &= \sqrt{20} \quad \text{reject -} \end{aligned}$$

$$\therefore y = 2 \cdot \sqrt{20} \quad y = 2x$$

$$= \underline{\underline{8,94}}$$

QUESTION 10



10.1.	$\hat{A}_1 = x$	
	$\therefore \hat{D}_2 = x$	$\checkmark SR$ alt "s =, $AC \parallel FD$
	$\therefore \hat{E}_1 = x$	$\checkmark \checkmark R^A$ tan chord
	$\therefore \hat{A}_1 = \hat{E}_1$	both = x
	$\therefore ABDE$ is a cyclic quad	\checkmark long "s in same segment = 4
10.2.	$\hat{D}_1 = x$	$\checkmark SF$ "s opp = sides
	$\therefore \hat{C} = x$	$\checkmark SR$ corr "s =, $AC \parallel FD$
	$\therefore \hat{C} = \hat{A}_1$	both = x

SR

$\therefore CD = AD$ ✓ sides opp = ^'s

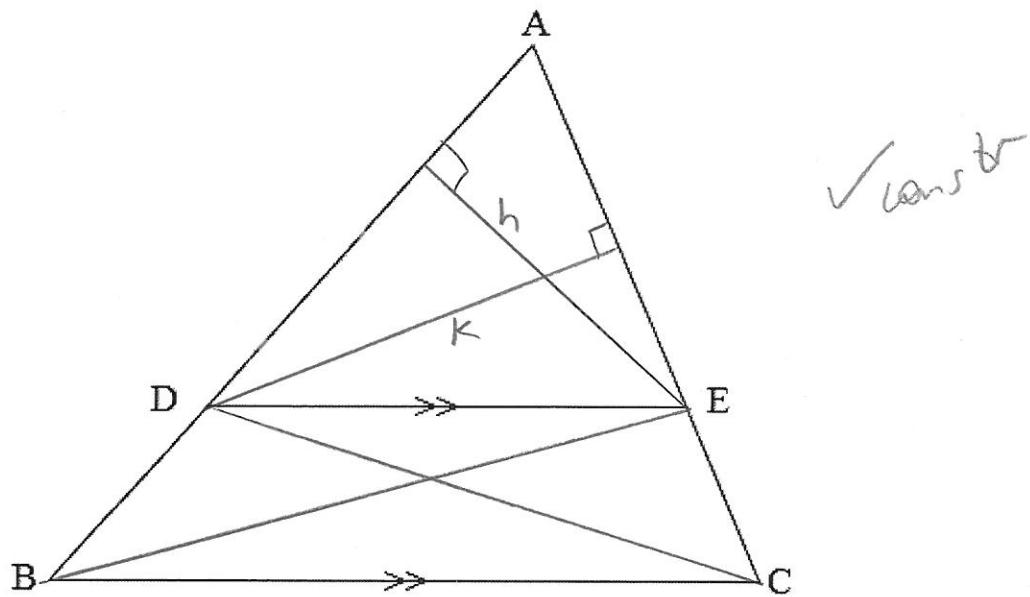
but $AD = AE$ ✓✓ tan's ext common
pt =

$\therefore AE = CD$  both = AD

5

QUESTION 11

11.1.



$$\frac{\text{area } \triangle ADE}{\text{area } \triangle DBE} = \frac{\frac{1}{2} AD \cdot h}{\frac{1}{2} DB \cdot h} = \frac{AD}{DB} \quad \checkmark$$

$$\frac{\text{area } \triangle AED}{\text{area } \triangle ECD} = \frac{\frac{1}{2} AE \cdot k}{\frac{1}{2} EC \cdot k} = \frac{AE}{EC} \quad \checkmark$$

• $\text{area } \triangle ADE = \text{area } \triangle AED$

same Δ

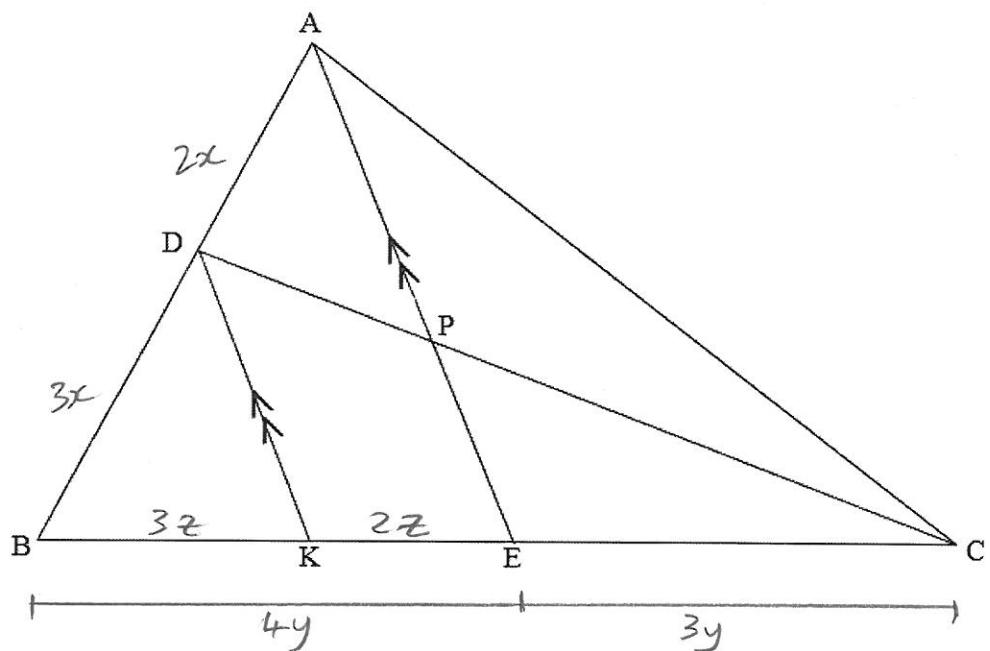
• $\text{area } \triangle DBE = \text{area } \triangle ECD \quad \checkmark$

$\checkmark \left\{ \begin{array}{l} \text{same base (DE)} \\ \text{same height (DE} \parallel BC) \end{array} \right.$

$\checkmark \left\{ \begin{array}{l} \text{same base (DE)} \\ \text{same height (DE} \parallel BC) \end{array} \right.$

	$\therefore \frac{\text{area } \triangle ADE}{\text{area } \triangle DBE} = \frac{\text{area } \triangle AED}{\text{area } \triangle ECD}$ ✓	
	$\therefore \frac{AD}{DB} = \frac{AE}{EC}$ 	6

11.2.



$$\frac{BK}{KE} = \frac{BD}{DA} \quad \checkmark \text{ line } l \parallel \text{ side of } \Delta$$

$$= \frac{3}{2} \checkmark^S \quad \text{fill in } 3z \ 2z$$

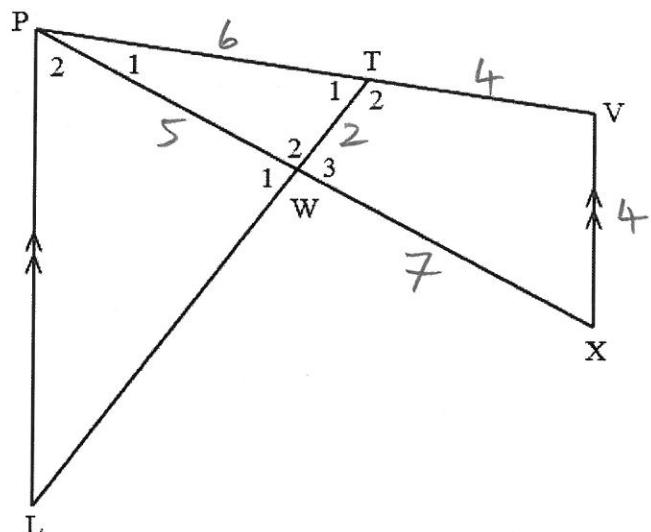
$$\frac{CP}{PD} = \frac{CE}{EK} \sqrt{SF} \text{ line } || \text{ side of } \Delta$$

$$= \frac{3y}{2z}$$

$$= \frac{3\left(\frac{5}{4}z\right)}{2z} \quad \frac{5}{4}z = 4y$$

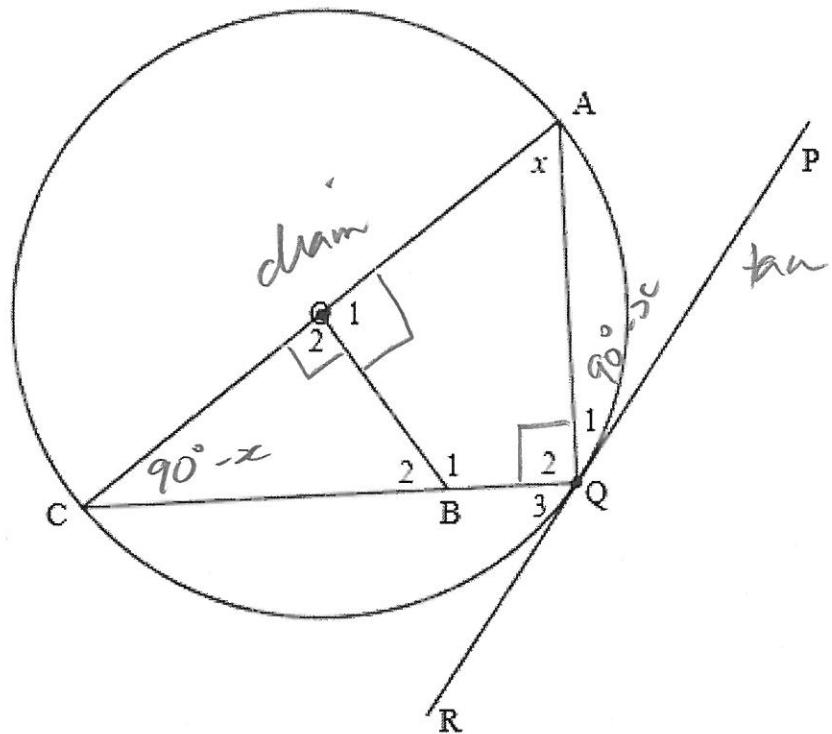
$$= \frac{15}{8}$$

QUESTION 12



12.1.	Given Δ 's PTW, PXV	
	1. $\frac{PT}{PX} = \frac{6}{12} = \frac{1}{2}$ ✓	
	2. $\frac{TW}{XV} = \frac{2}{4} = \frac{1}{2}$ ✓	
	3. $\frac{WP}{VP} = \frac{5}{10} = \frac{1}{2}$ ✓	
	$\therefore \frac{PT}{PX} = \frac{TW}{XV} = \frac{WP}{VP} = \frac{1}{2}$ ✓ R	
	$\therefore \underline{\Delta \text{PTW} \parallel\!\!/\! \Delta \text{PXV}}$ sides of Δ in prop^n 4	
12.2.	$\hat{P}_2 = \hat{X}$ ✓ ^{SR} alt "s =, PL VX	
	$= \hat{T}_1$ ✓ ^{SR} $\underline{\Delta P_1 T_1 W_2 \parallel\!\!/\! \Delta P_1 X V}$	
	$\therefore \hat{P}_2 = \hat{T}_1$ ✓ ^S both = \hat{X}	
	\therefore PL is a \checkmark conv ^ tan chord	
	<u>tangent</u> →	4

QUESTION 13



13.1.	$\hat{O}_1 = 90^\circ$ given $\hat{Q}_2 = 90^\circ$ ✓ ✓ \wedge in semi $\odot = 90^\circ$ $\therefore \hat{O}_1 + \hat{Q}_2$ $= 90^\circ + 90^\circ$ $= 180^\circ$ ✓ ✓ R $\therefore \underline{\text{BOAQ is a cyclic quad}} \rightarrow \underline{\text{opp } \wedge \text{'s cyclic quad}} = 180^\circ$ L
13.2.	$\hat{C} = 90^\circ - x$ ✓ SR $\wedge \Delta = 180^\circ$ $\hat{Q}_1 = 90^\circ - x$ ✓ SR \wedge tan chord 2 \rightarrow

13.3.	1. In Δ 's $C B_2 O_2, C A Q_2$	
	1. $\hat{C} = \hat{C}$ ✓ SR common	
	2. $\hat{O}_2 = \hat{Q}_2$ ✓ S both = 90°	
	$\therefore \Delta CBO \sim \Delta CAQ \xrightarrow{\text{AAA}} \text{AAA} \sqrt{R}$	3
13.3.	2. $\frac{CB}{CA} = \frac{CO}{CQ} \sqrt{SR} \quad \Delta \widehat{CBO} \sim \Delta \widehat{CAQ}$	
	$\therefore CB \cdot CQ = CO \cdot CA \checkmark$	
	$= CO \cdot (2CO) \checkmark \text{S radius}$	
	$= 2 CO^2 \checkmark \text{ cr}$	
	$= 2(CB^2 - OB^2) \checkmark \text{Pythag}$	
	$\underline{= 2CB^2 - 2OB^2}$	5